Verified Uncertainty Calibration

Ananya Kumar, Percy Liang, Tengyu Ma Stanford University









Uncertainties - Beyond Model Accuracy



Reality: 40% such people have cancer (!) Implication: Wrong Treatment

• Testicular cancer (Calster & Vickers), Bipolar disorder (Lindhiem et al), Criminal recidivism (Fazel et al)

Miscalibration of Neural Networks

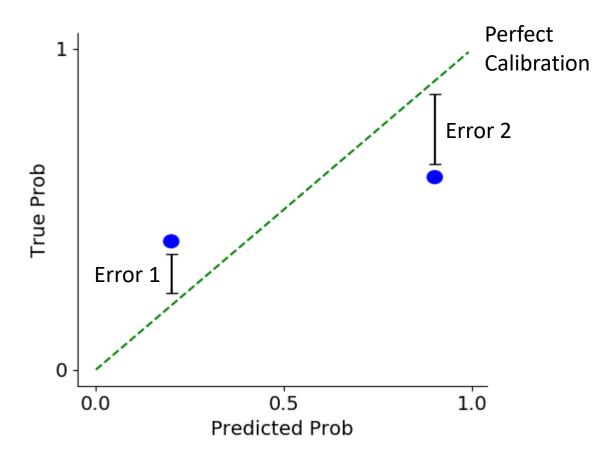
Resnet on CIFAR-100

Model's perceived accuracy	90%
Actual accuracy	70%

Cite: Guo et al 2017

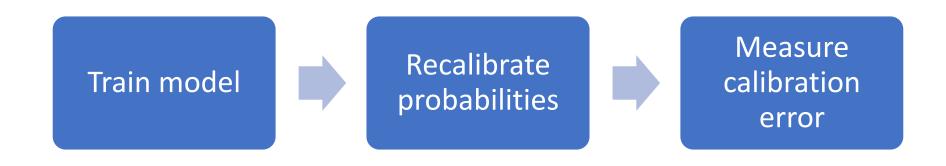
Calibration Error (CE)

Average difference between model's predicted prob and true prob



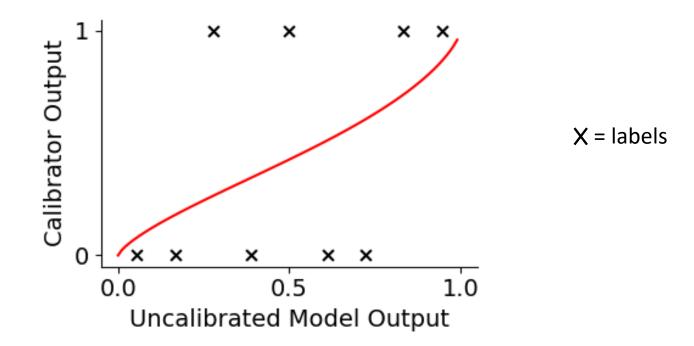
Details: $CE = \sqrt{E[(m-p)^2]}$ m is predicted prob p is true prob

Recalibration Pipeline



Platt Scaling

 Platt scaling, temperature scaling scale the model probabilities to improve them



1. Is Platt Scaling calibrated?

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- Prior work reports calibration error = 2%
- We show that calibration error greater than 4%

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Deep Model

Is Model' calibrated?

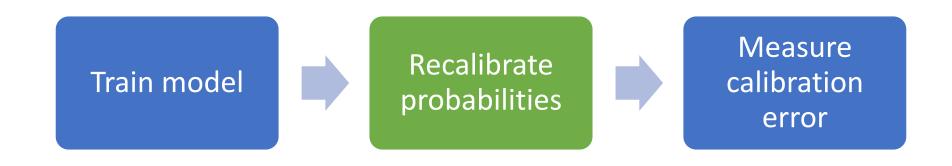
Platt Scaling

Model'

- Prior work reports calibration error = 2%
- We show that calibration error greater than 4%

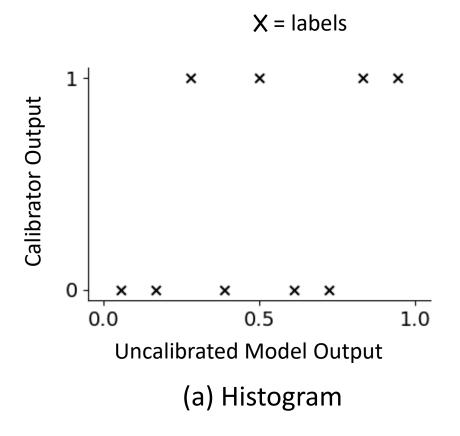
Impossible to measure calibration error of scaling

Recalibration Pipeline

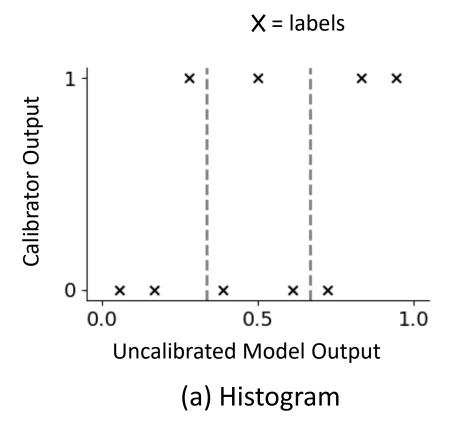


Should be able to tell how calibrated we are!

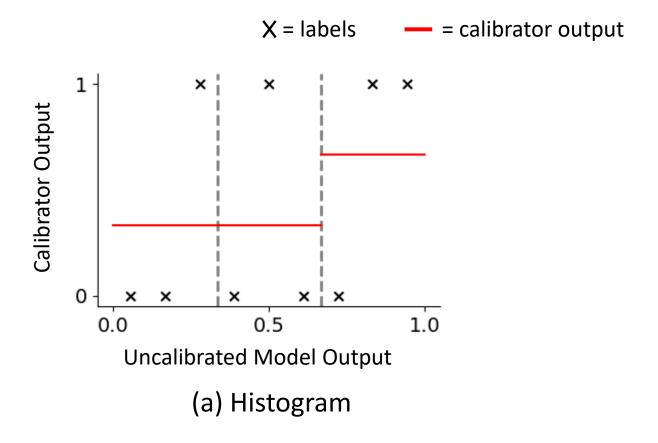
Histogram binning outputs average label value in each bin

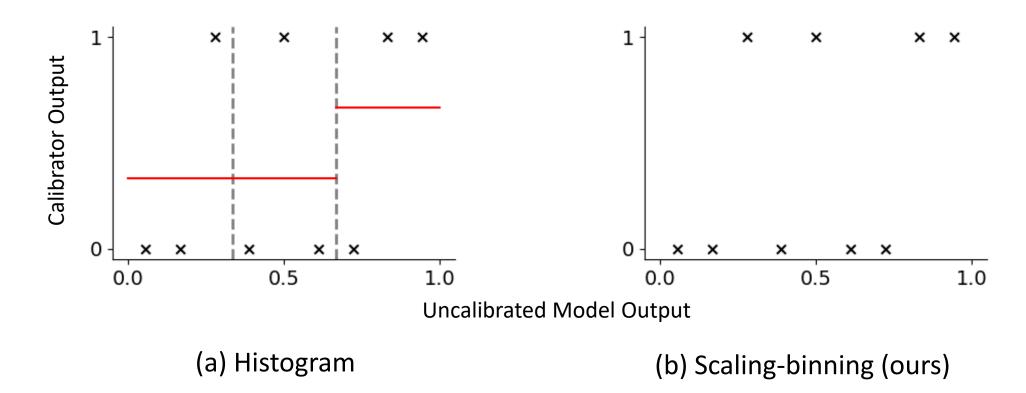


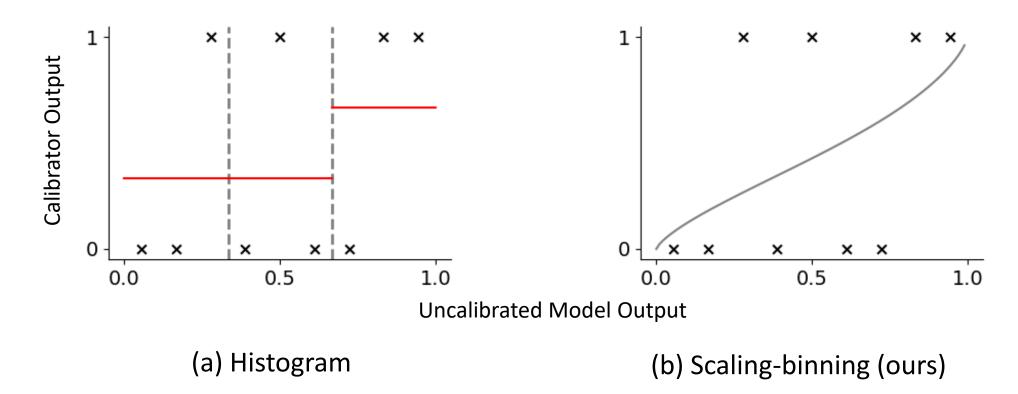
Histogram binning outputs average label value in each bin

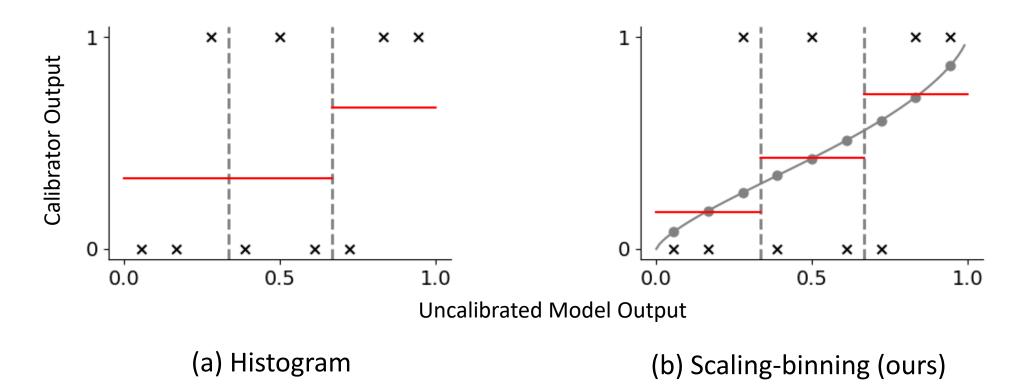


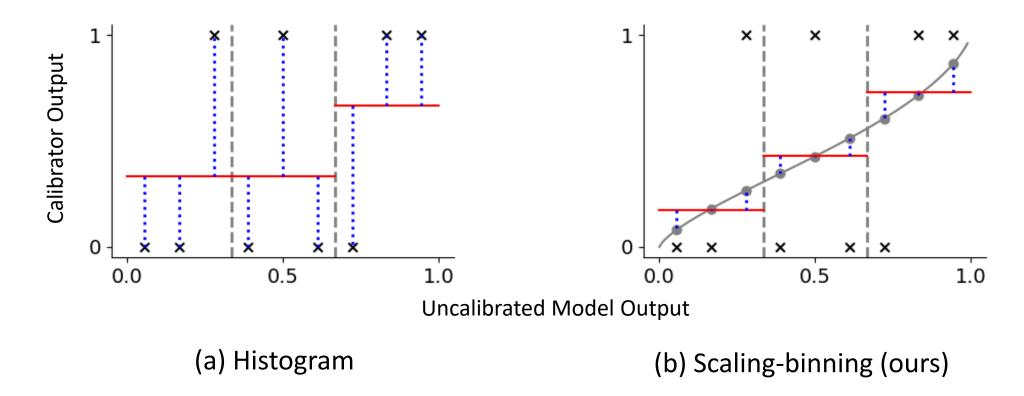
Histogram binning outputs average label value in each bin











Recalibration Method	Samples Needed	Can Estimate Calibration?
Platt Scaling	Few: $O\left(\frac{1}{\varepsilon^2}\right)$	×

B = # Bins ε = desired CE

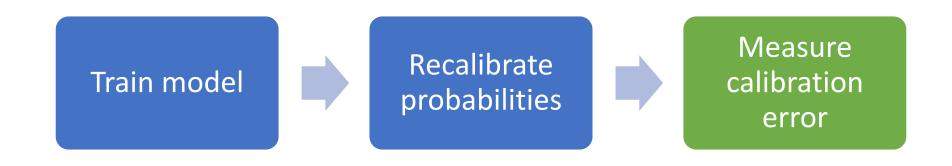
Recalibration Method	Samples Needed	Can Estimate Calibration?
Platt Scaling	Few: $O\left(\frac{1}{\varepsilon^2}\right)$	×
Histogram Binning	More: $O\left(\frac{B}{\varepsilon^2}\right)$	√

B = # Bins ε = desired CE

Recalibration Method	Samples Needed	Can Estimate Calibration?
Platt Scaling	Few: $O\left(\frac{1}{\varepsilon^2}\right)$	×
Histogram Binning	More: $O\left(\frac{B}{\varepsilon^2}\right)$	
Scaling-Binning (Ours)	Few: $O\left(\frac{1}{\varepsilon^2} + B\right)$	

B = # Bins ε = desired CE

Recalibration Pipeline

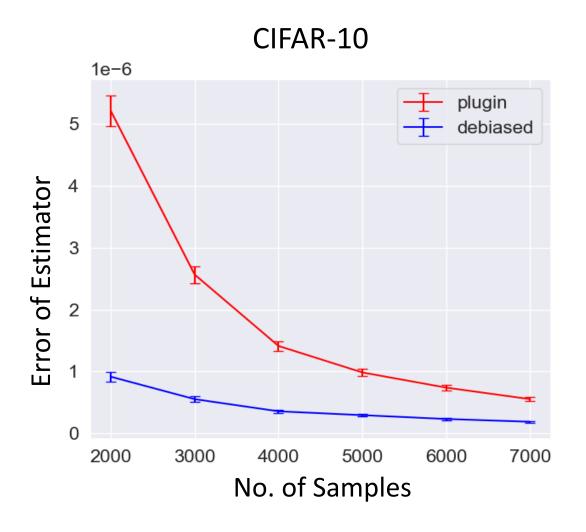


3. Verifying Calibration

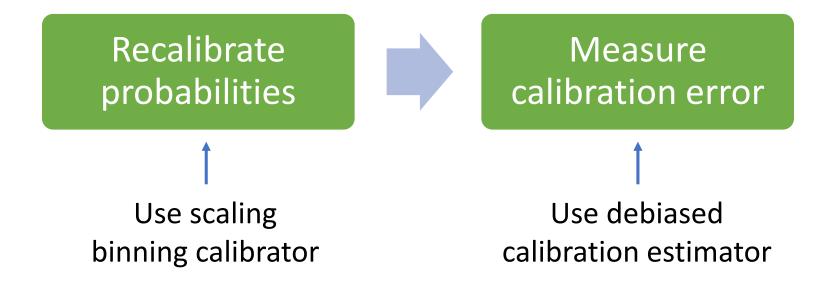
- Plugin: standard, everyone uses it (just average)
- Debiased: more sophisticated estimator from meteorology community

Estimation Method	Samples Needed
Plugin	More: $O\left(\frac{B}{\varepsilon^2}\right)$
Debiased	Fewer: $O\left(\frac{\sqrt{B}}{\varepsilon^2}\right)$

3. Verifying Calibration



Takeaways



- For scaling methods: can only lower bound calibration error
 - Still use debiased estimator: estimates lower bound with fewer samples

Calibration Library

- Code at https://github.com/AnanyaKumar/verified calibration
- Measure model accuracy and calibration

```
pip install uncertainty-calibration
```

```
import calibration as cal
ce = cal.get_calibration_error(logits, labels)
```

Poster #54

East Exhibition Hall B + C
TODAY 10:45am